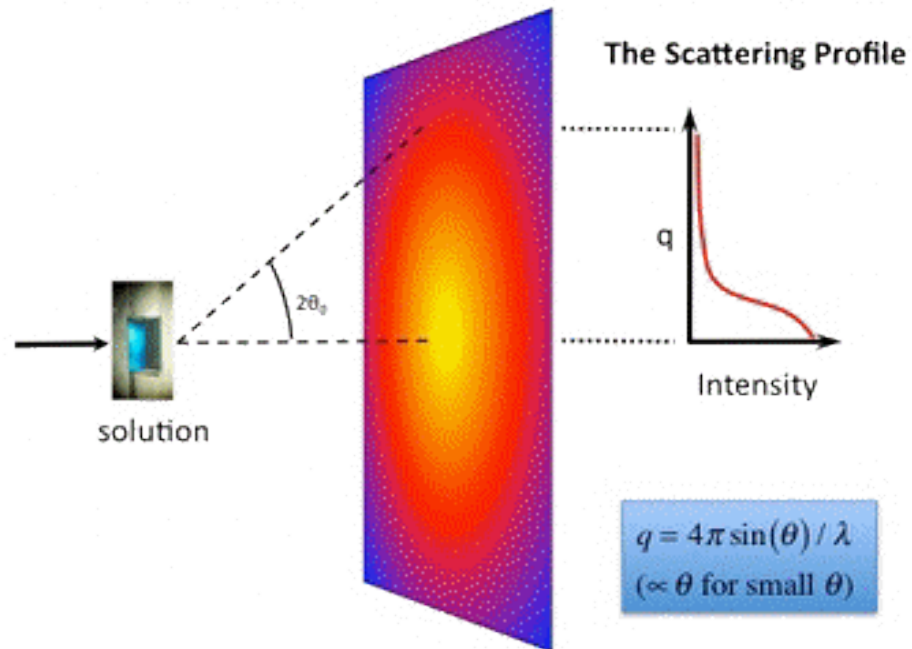
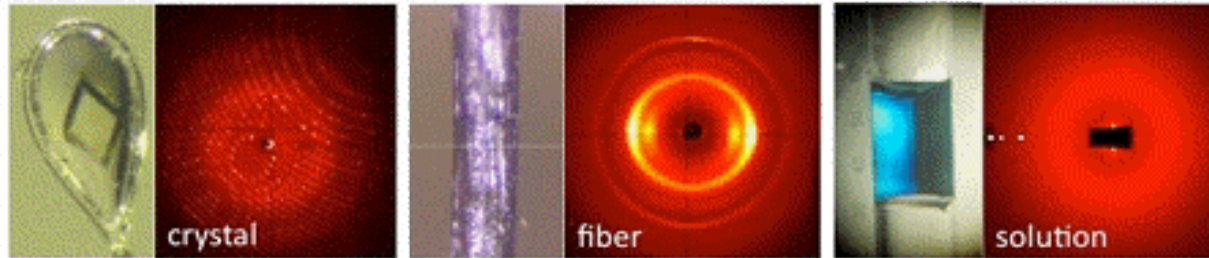
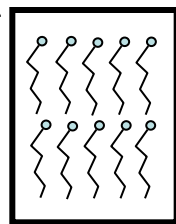
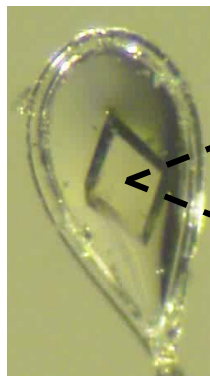
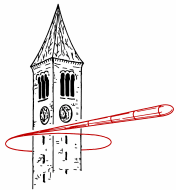


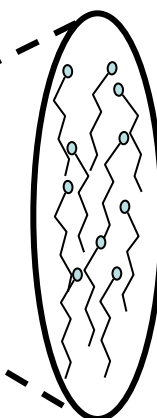
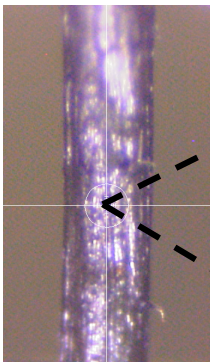
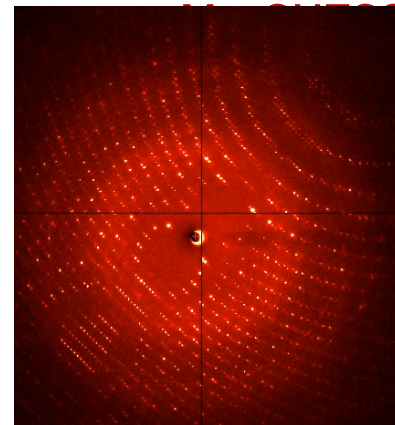
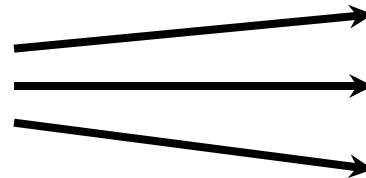
BioSAS Overview and Applications

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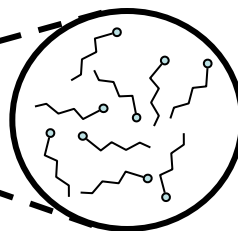
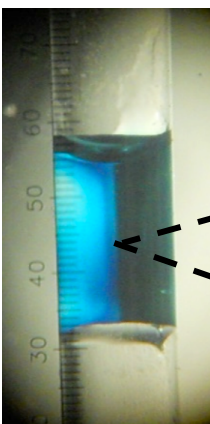
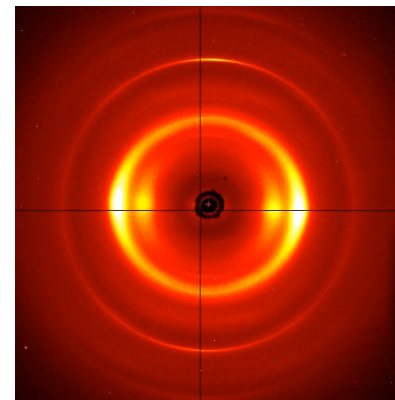
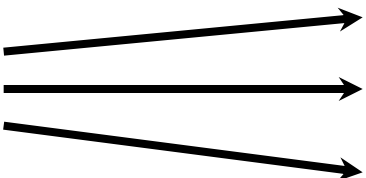




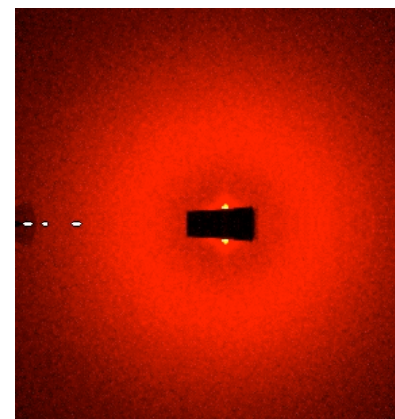
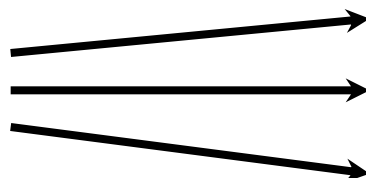
crystal

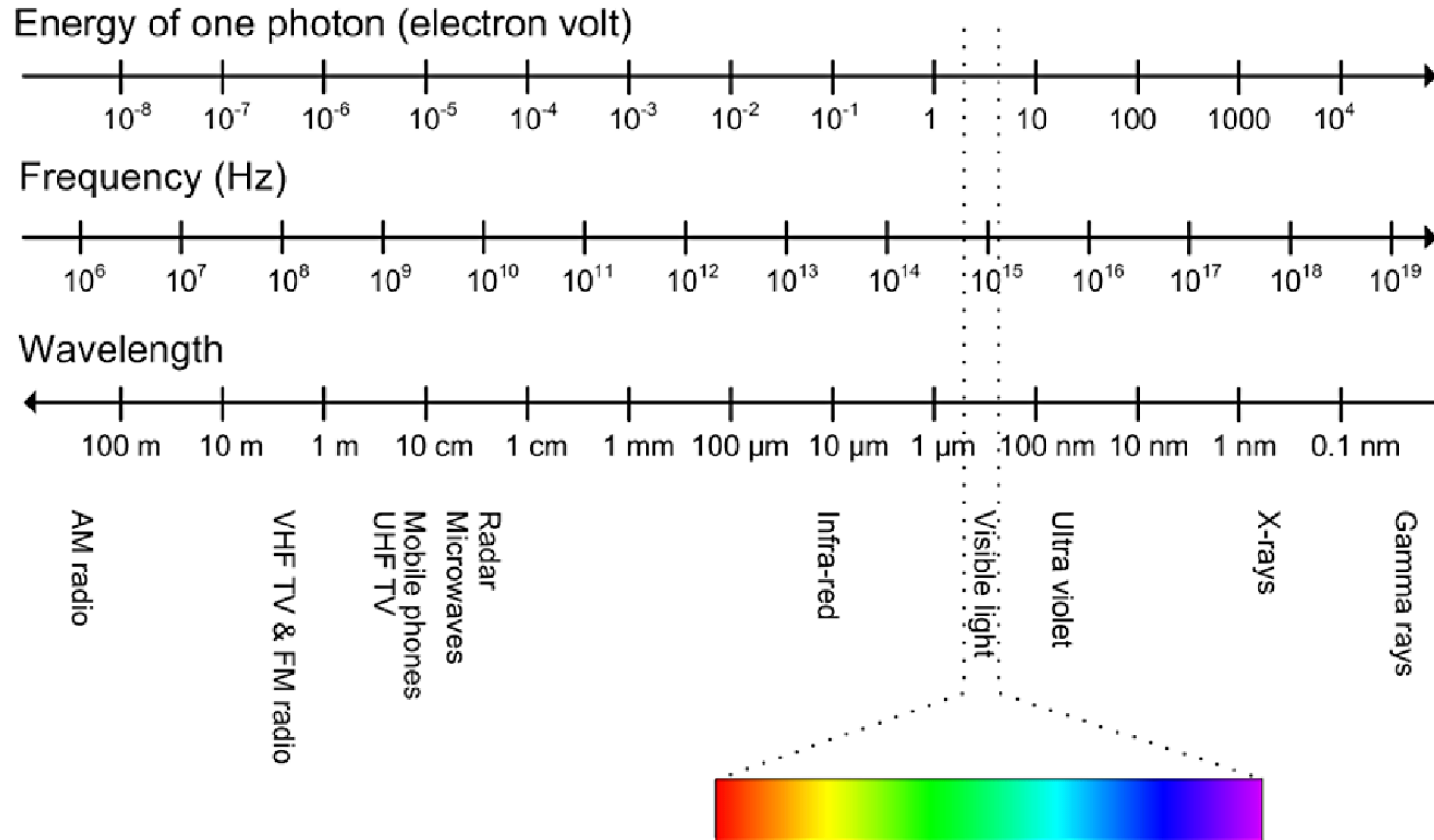
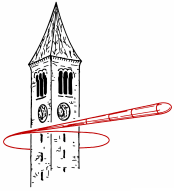


fiber



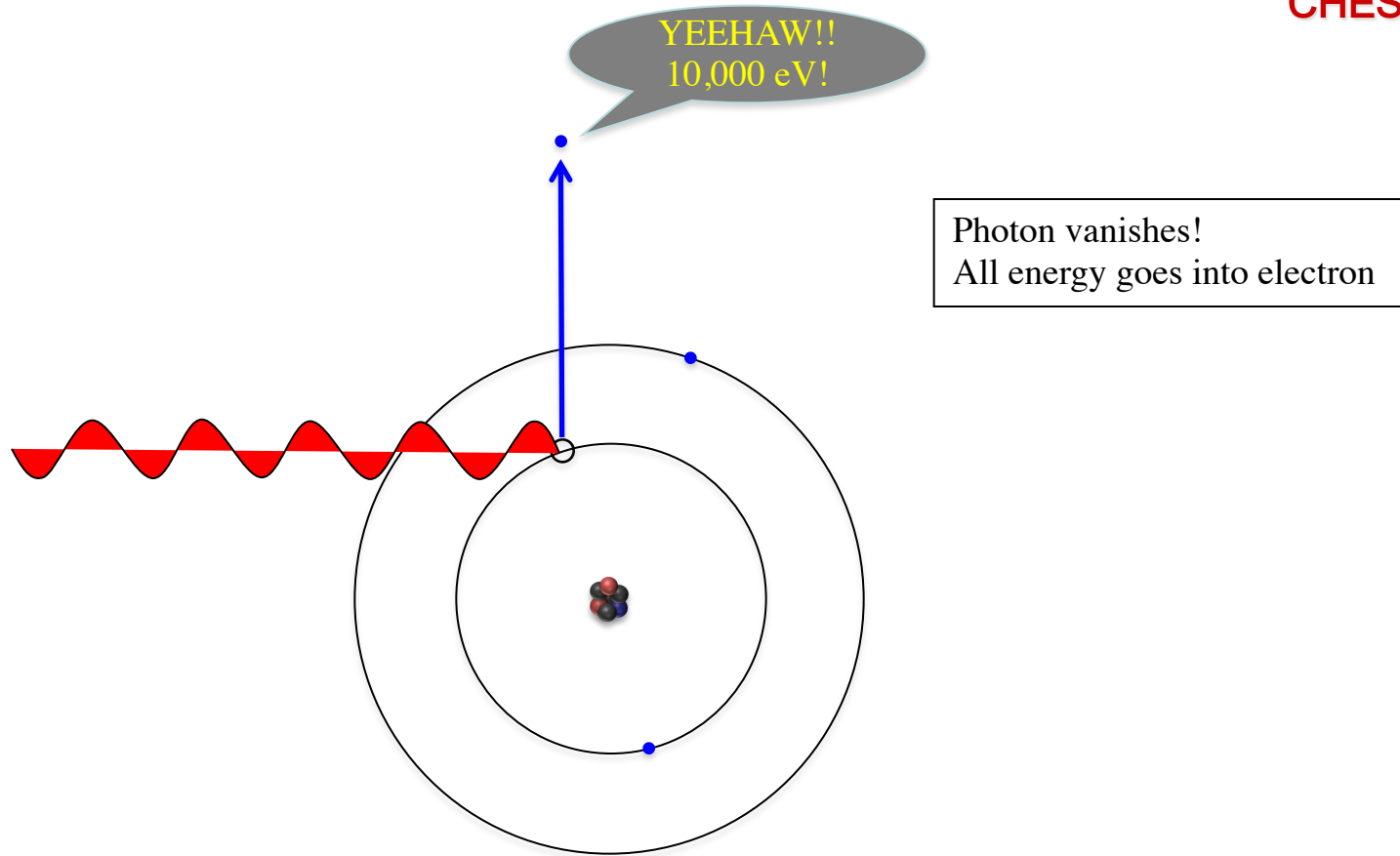
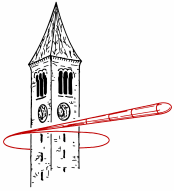
solution



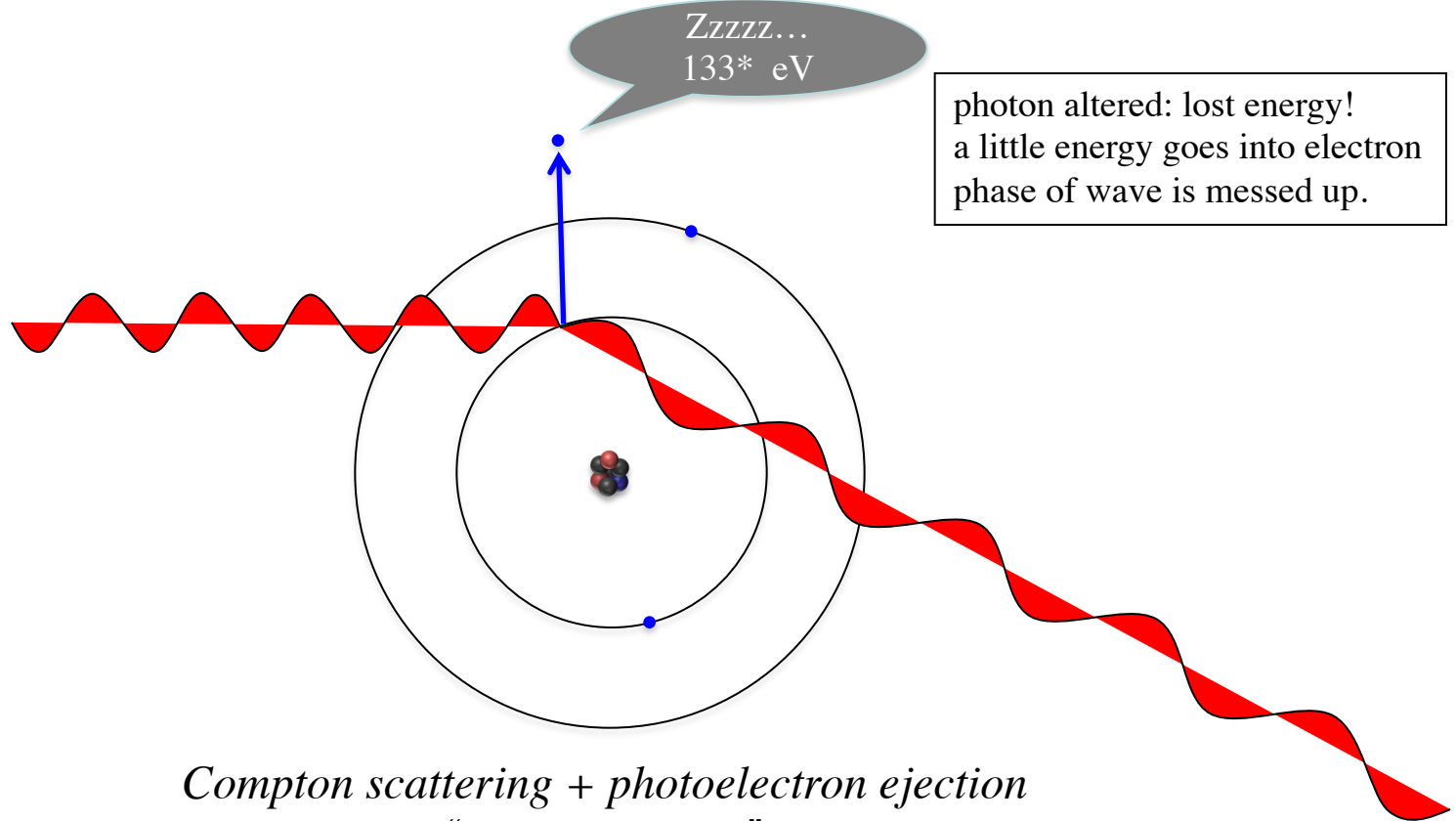
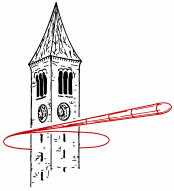


Useful: Energy (keV) = 12.4/wavelength (Angstroms)

* From <http://what-when-how.com/wp-content/uploads/2012/07/tmp26dc54.png>

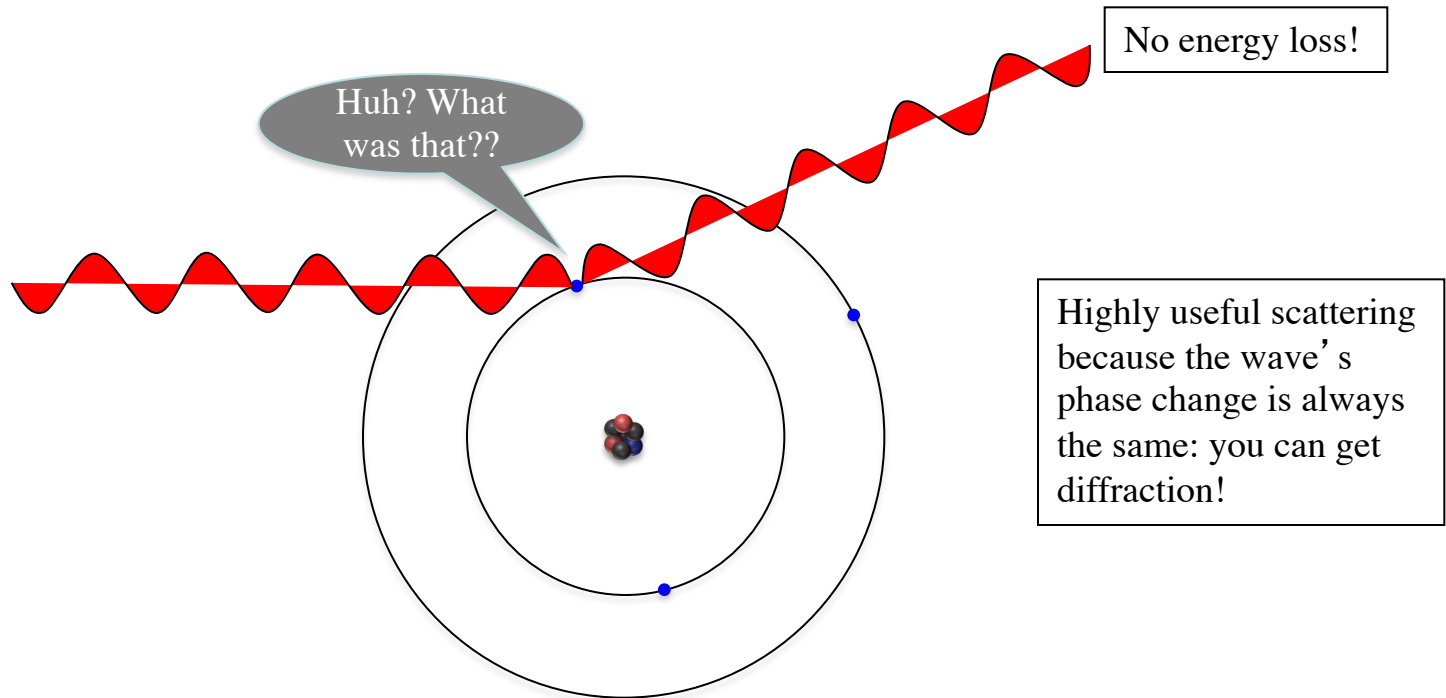
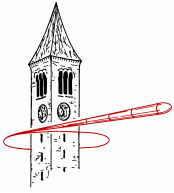


Photoabsorption → photoelectron ejection → fluorescence



Compton scattering + photoelectron ejection
“modified scattering”

* Compton $\Delta E @ 90^\circ = 188 \text{ eV}$
Lithium 1s binding = 54.7 eV
 $188 \text{ eV} - 54 \text{ eV} = 133 \text{ eV}$

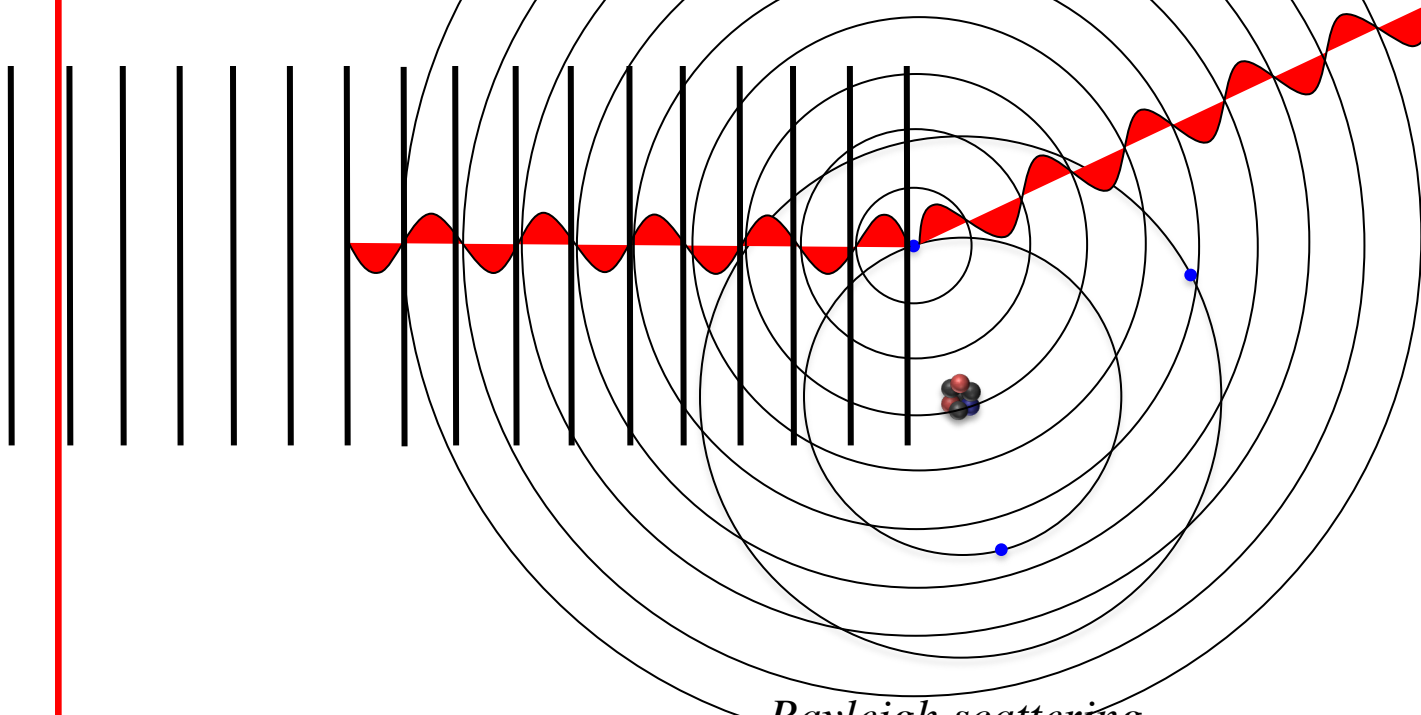
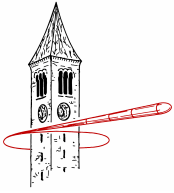


Rayleigh scattering
“unmodified scattering”

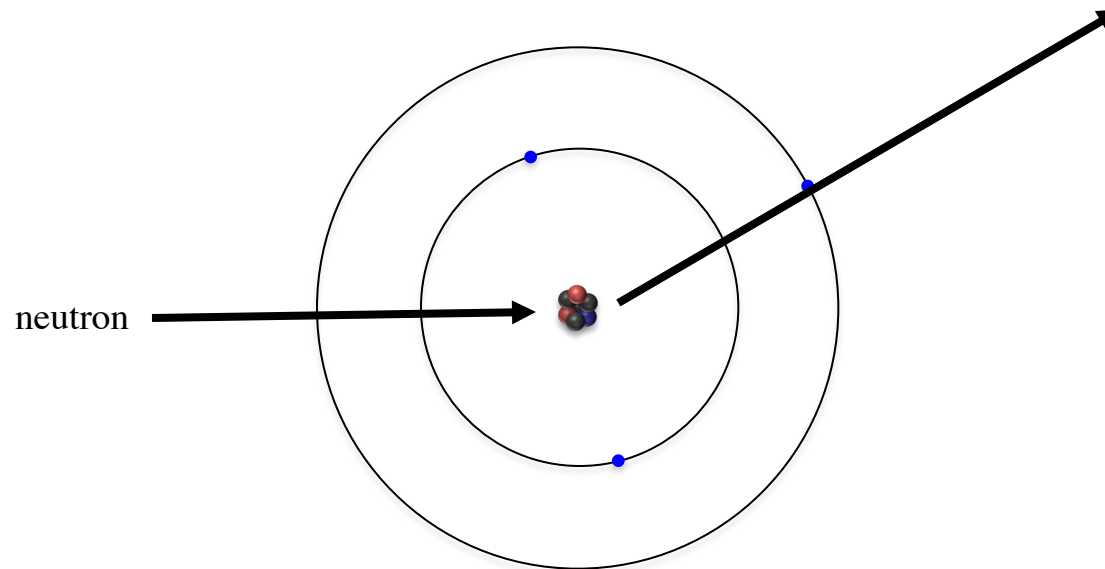
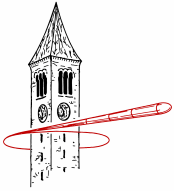
Rayleigh scattering = bound electron

Thomson scattering = free electron

To hard X-rays, everything looks like a free electron anyhow!

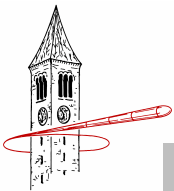


Rayleigh scattering
“unmodified scattering”



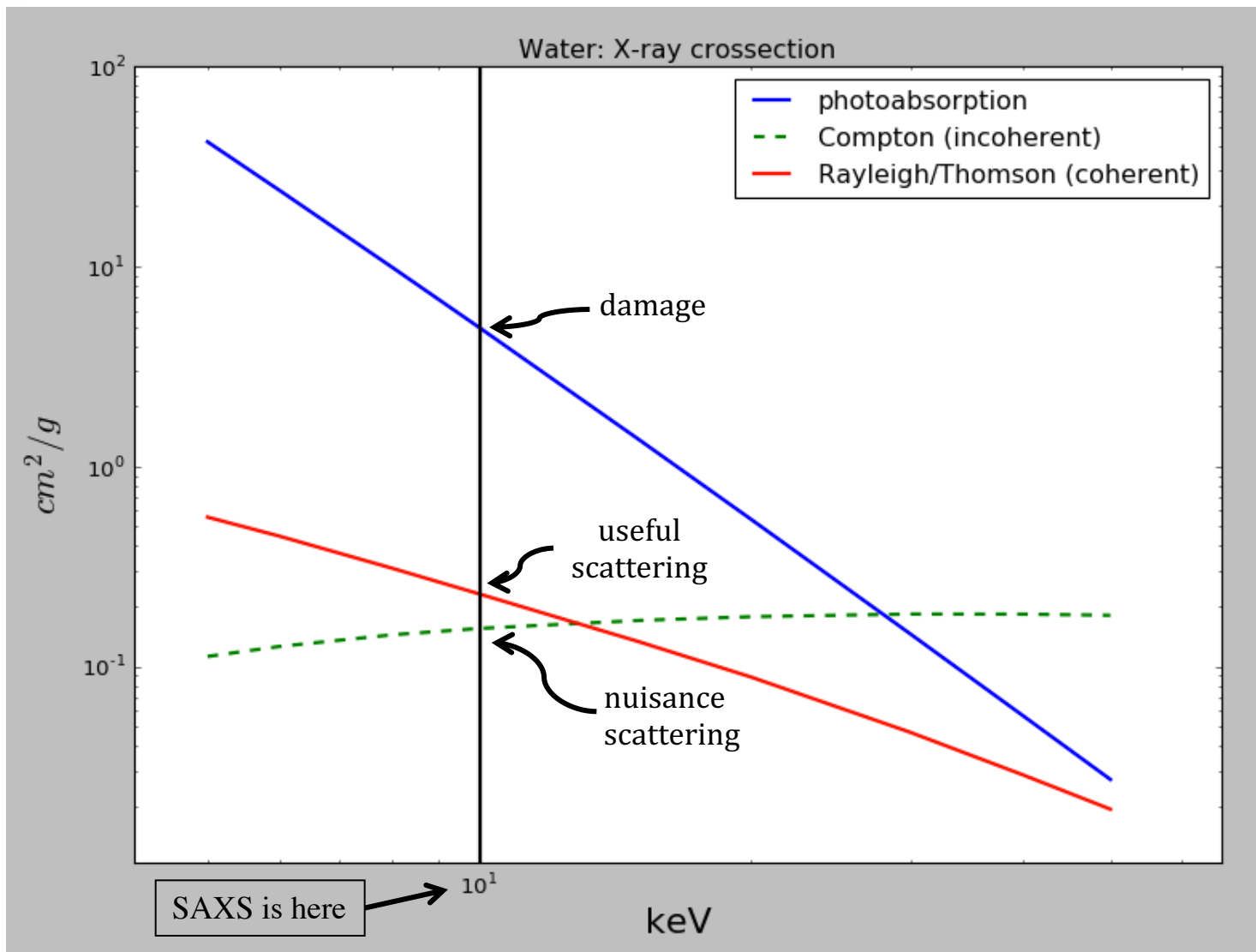
Scattering of **photons** by the nucleus does happen, it's just far too weak to observe.
Neutrons, on the other hand, are scattered by the nucleus very effectively: SANS!

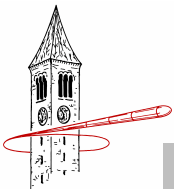
**when photon Energy > 1 MeV: photonuclear effects, pair production, Delbrück scattering etc.*



Energy and X-ray Damage

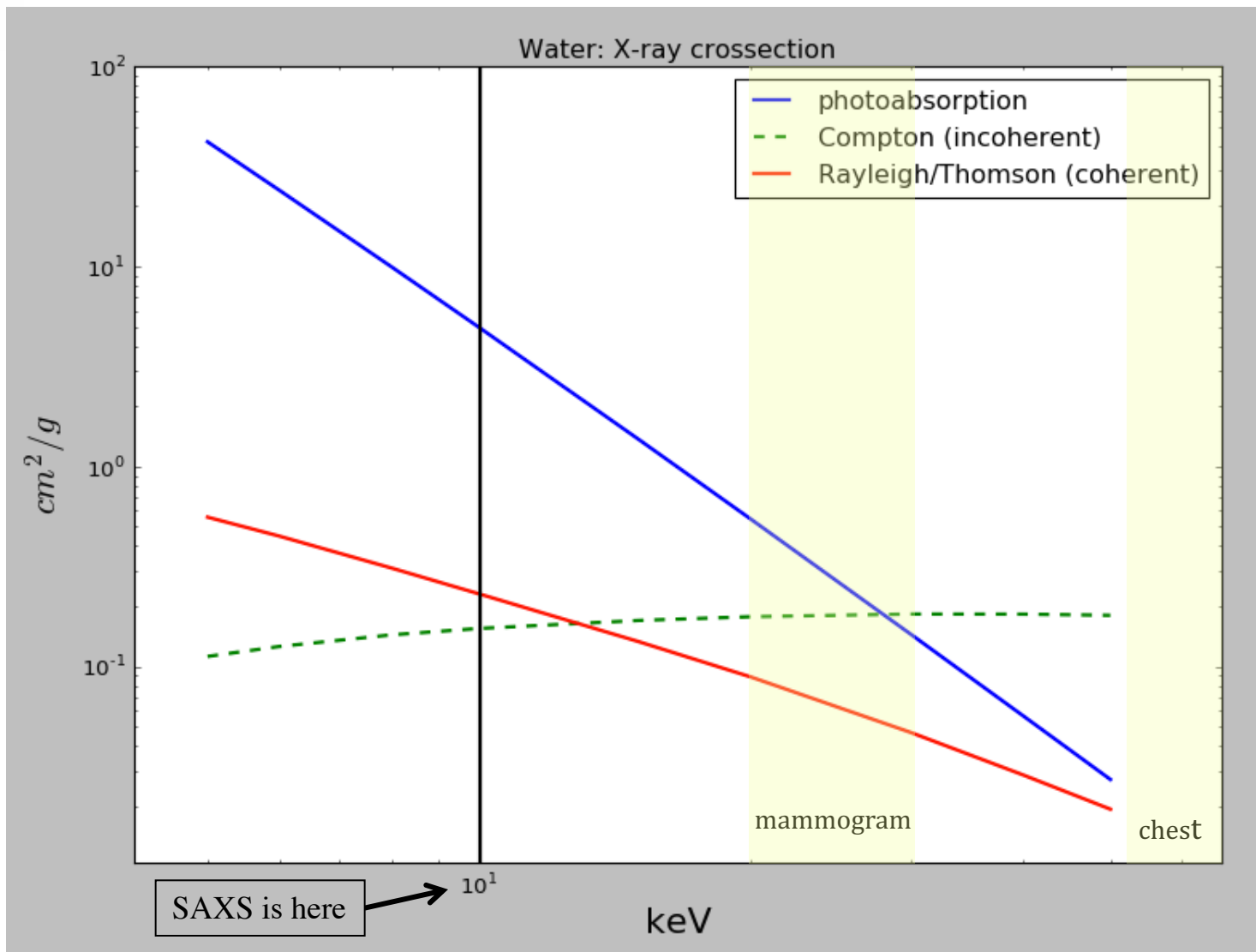
MacCHESS
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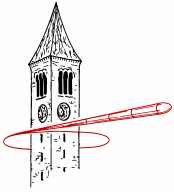




The sad reality of biology with X-rays

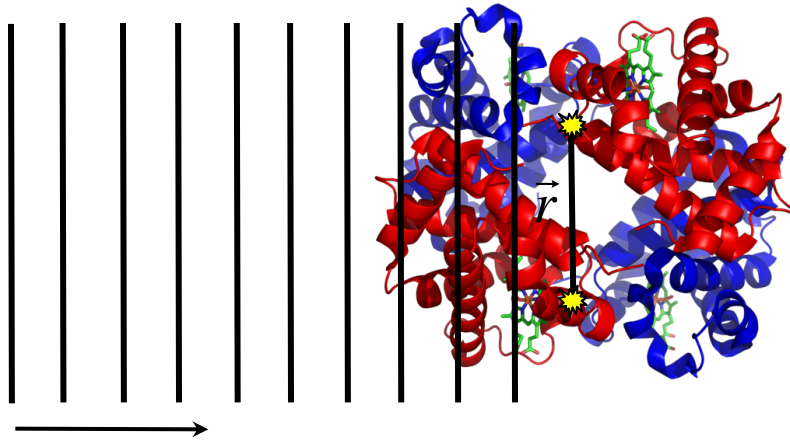
MacCHESS
CHESS

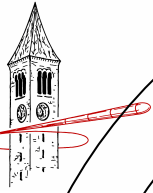




Diffraction from a single molecule

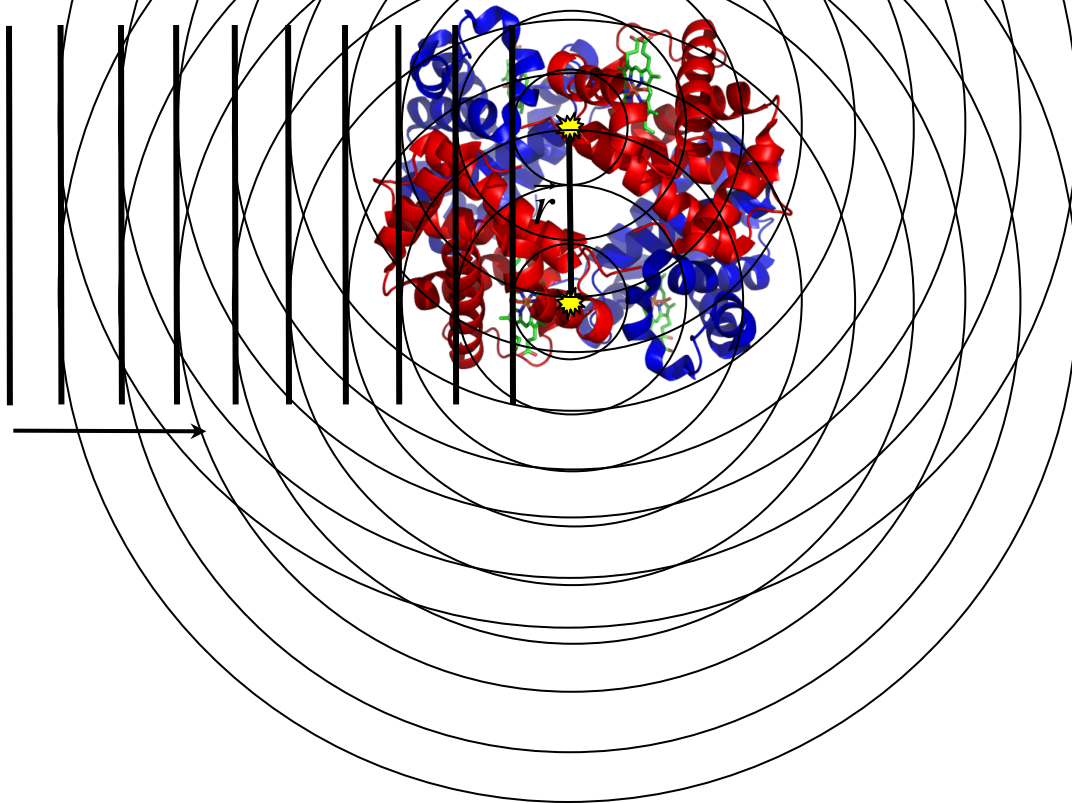
MacCHESS
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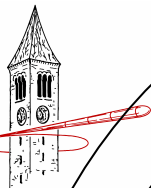




Diffraction from a single molecule

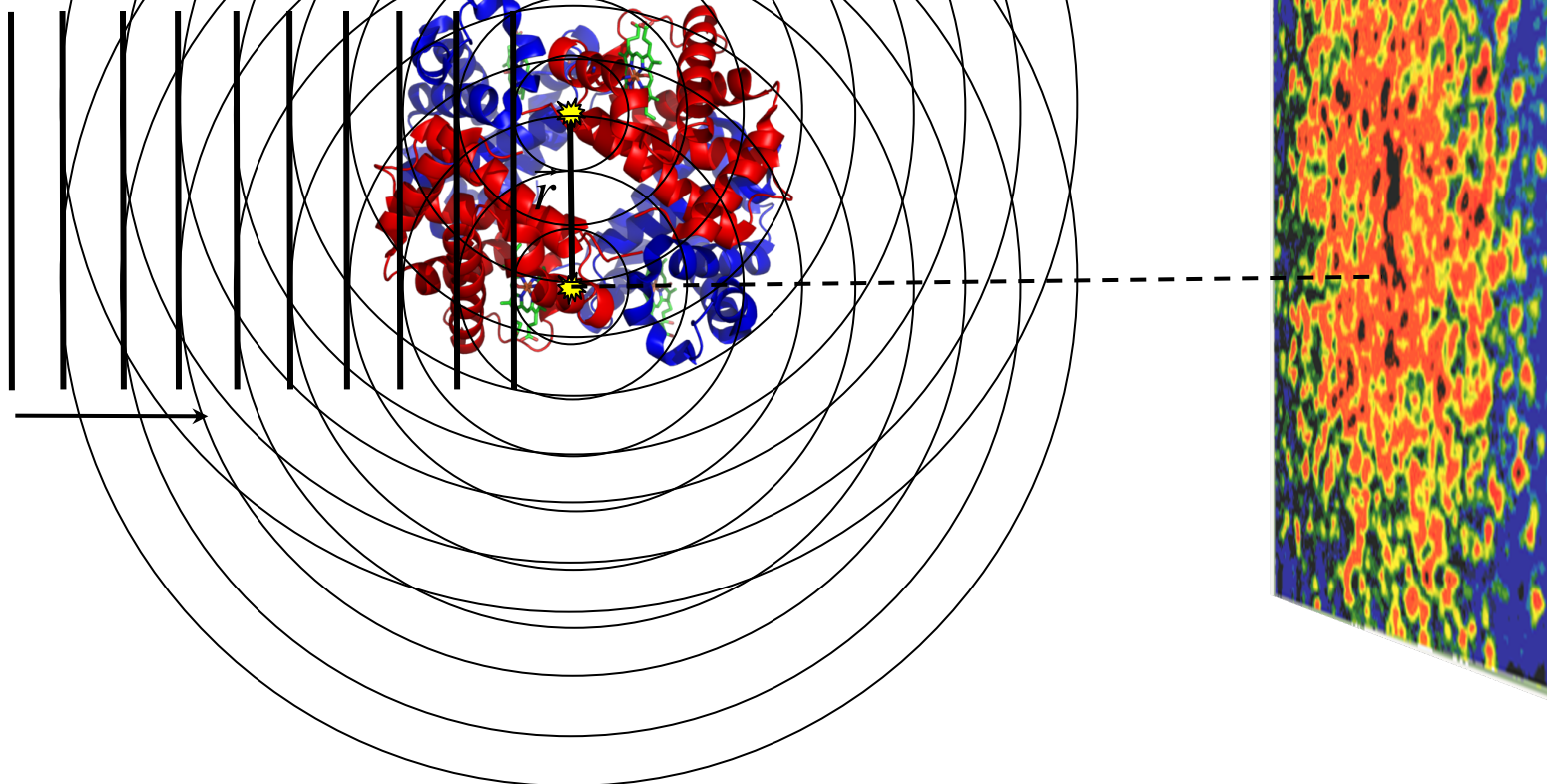
MacCHESS
CHESS

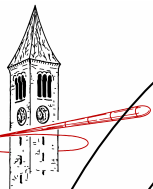




Diffraction from a single molecule

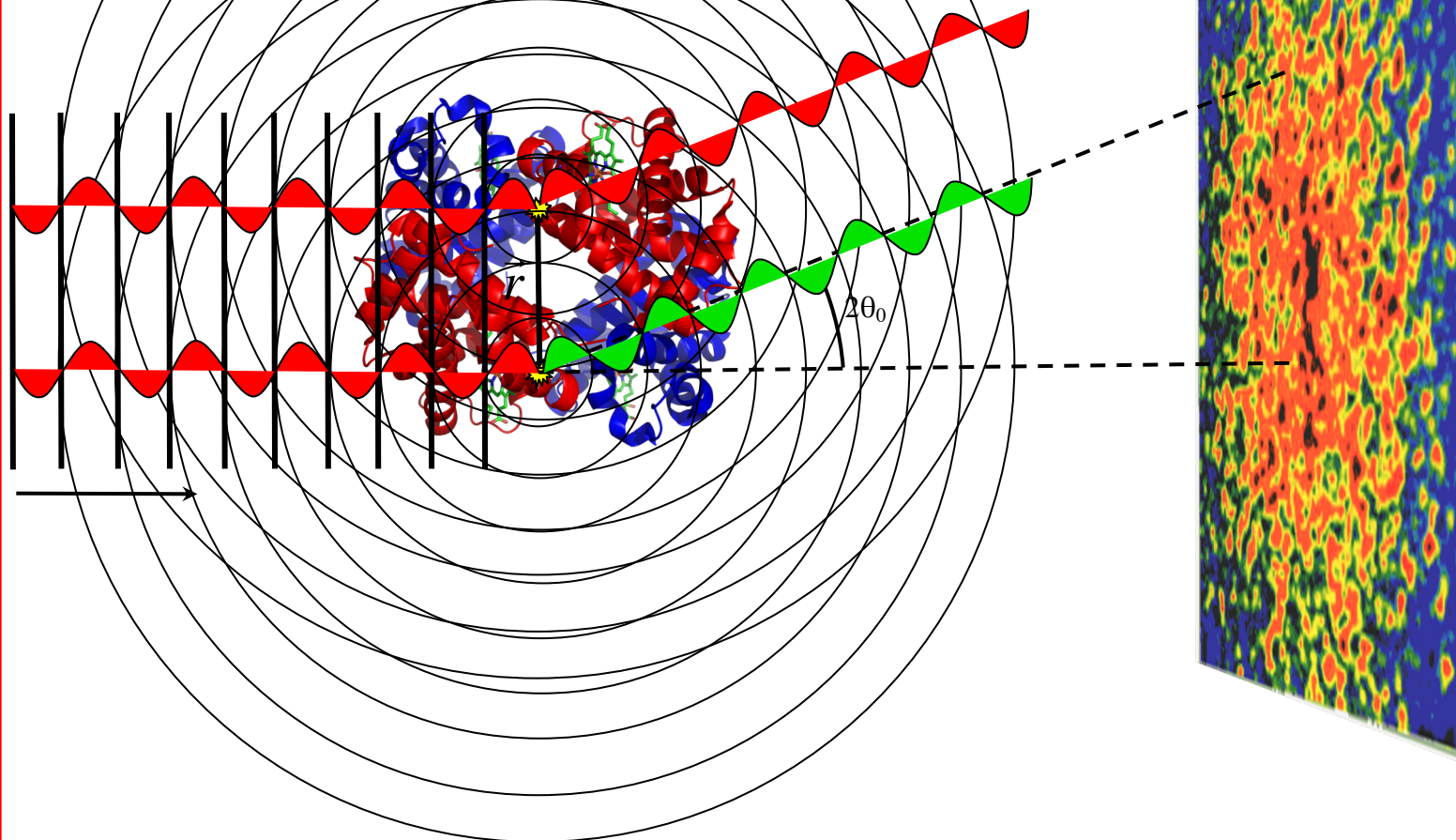
MacCHESS
CHESS

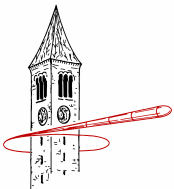




Diffraction from a single molecule

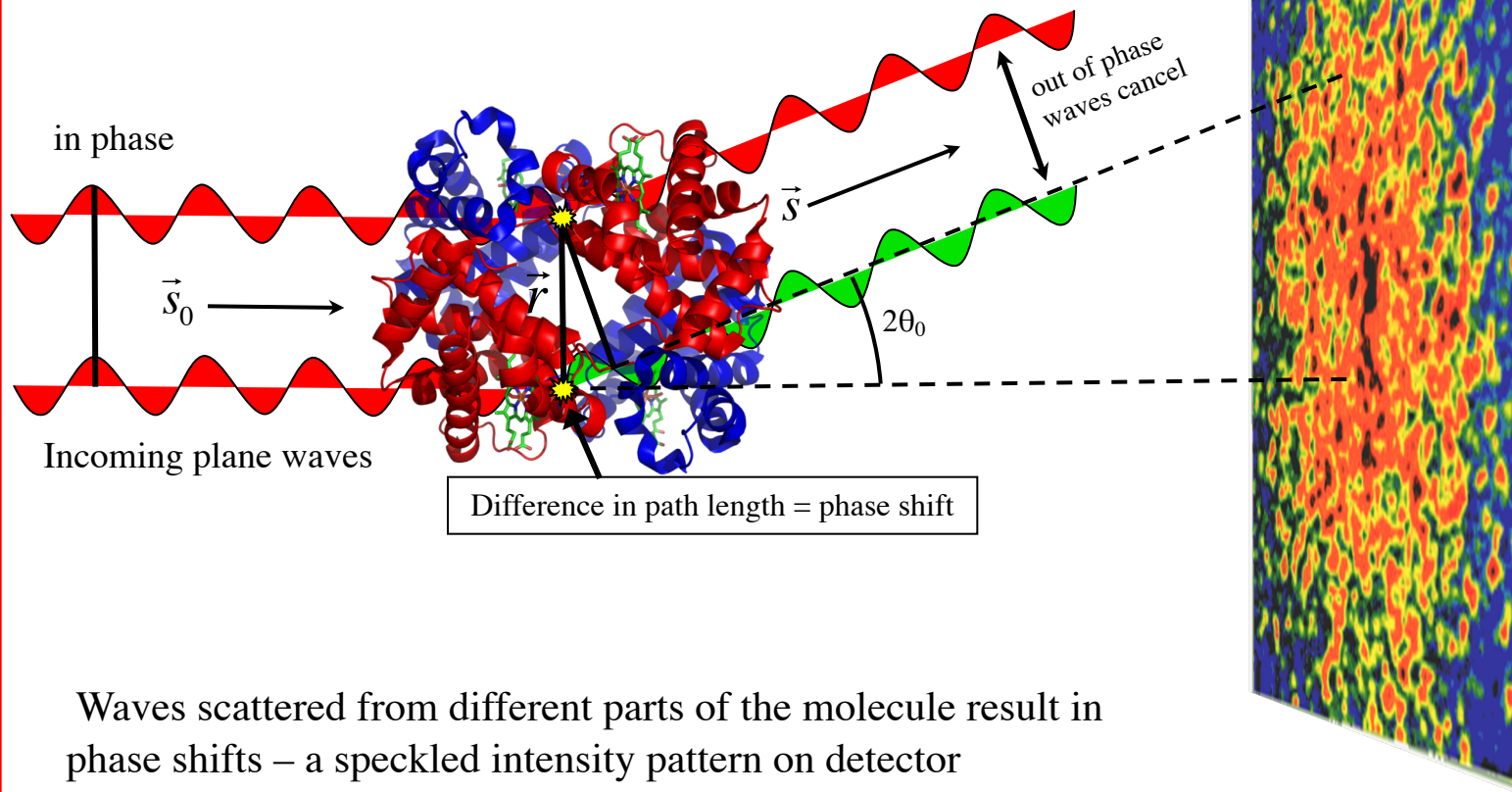
MacCHESS
CHESS





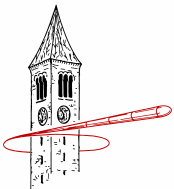
Diffraction from a single molecule

MacCHESS
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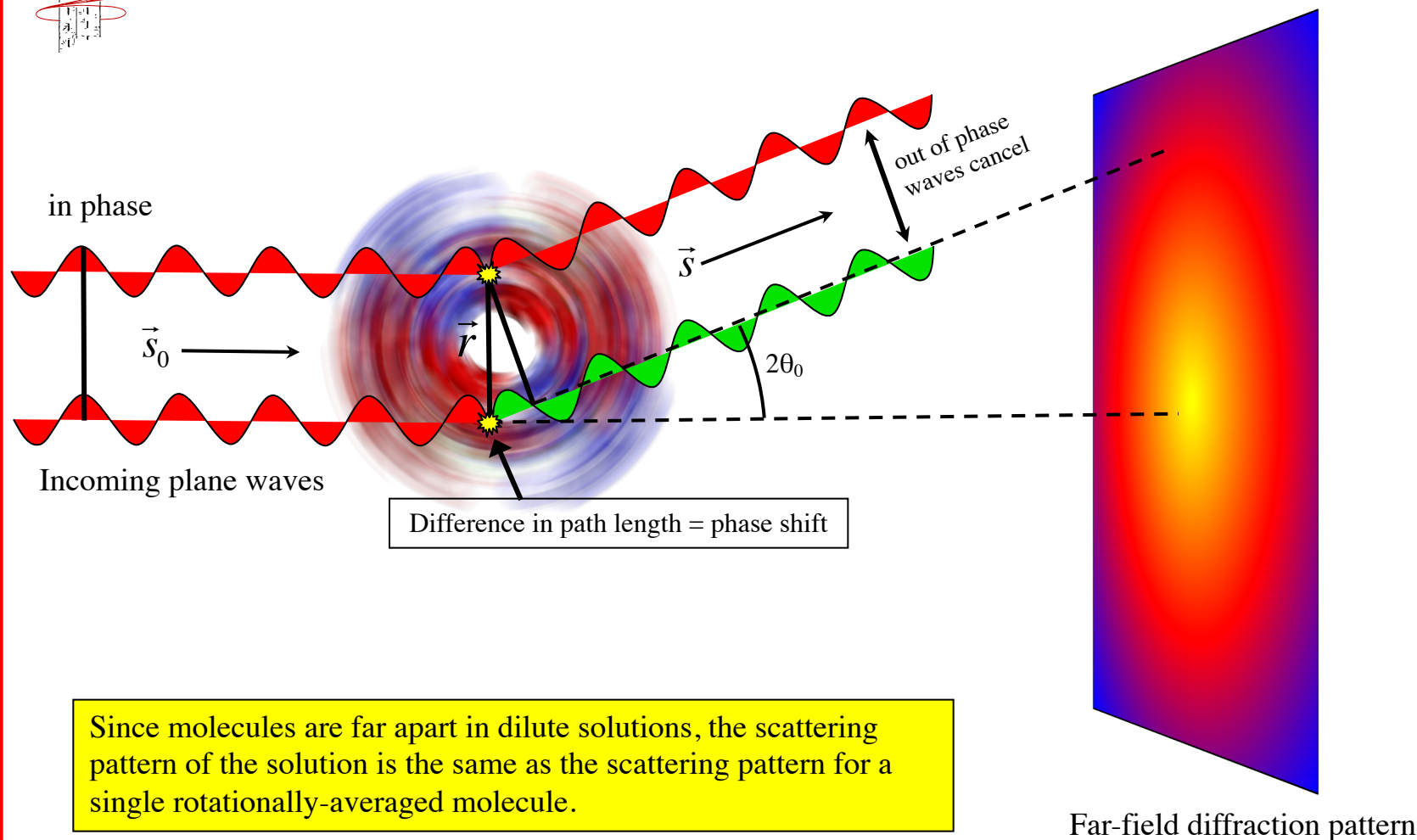
Waves scattered from different parts of the molecule result in phase shifts – a speckled intensity pattern on detector

Far-field diffraction pattern

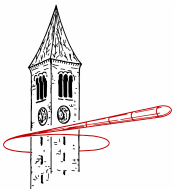


Diffraction from a rotationally-averaged molecule

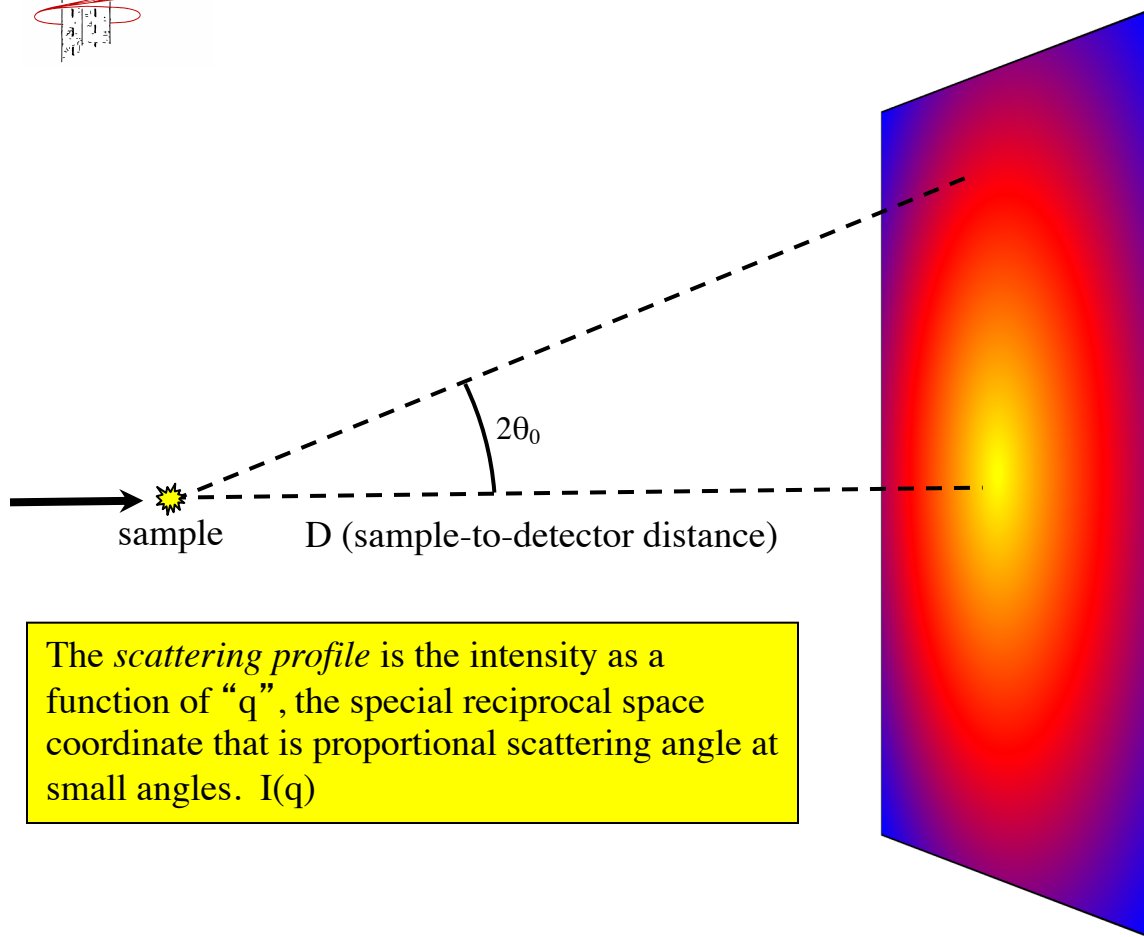
MacCHESS
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Since molecules are far apart in dilute solutions, the scattering pattern of the solution is the same as the scattering pattern for a single rotationally-averaged molecule.

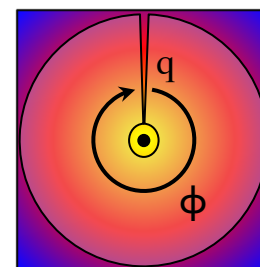
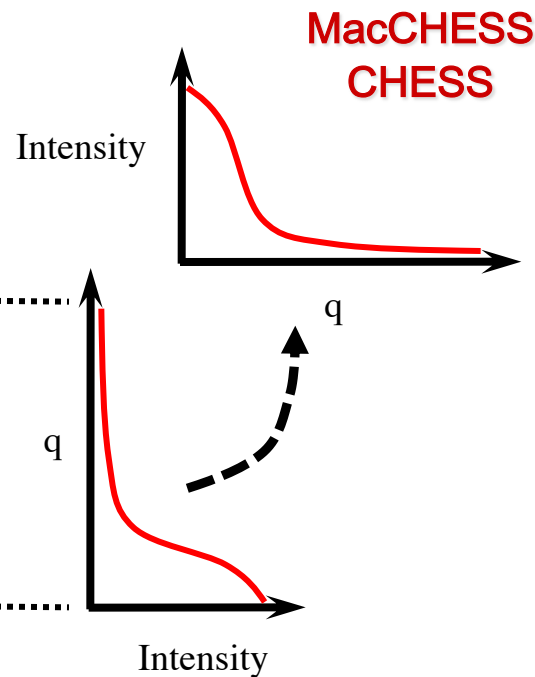


The Scattering Profile

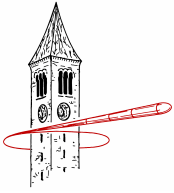


The *scattering profile* is the intensity as a function of “q”, the special reciprocal space coordinate that is proportional scattering angle at small angles. $I(q)$

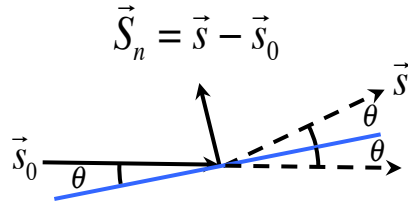
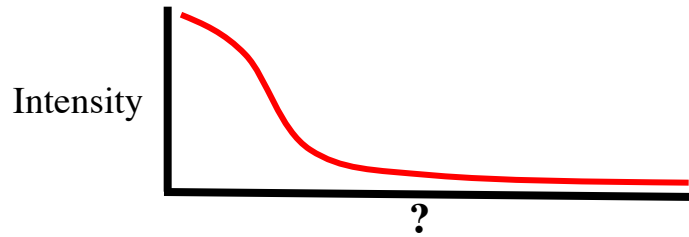
$$q = 4\pi \sin(\theta) / \lambda \quad (\propto \theta \text{ for small } \theta) \quad \text{Far-field diffraction pattern}$$



$I(q)$ is obtained by integrating around the circle. For detectors, the standard deviation of signal $\sigma(q)$ is also calculated.



Most important variable in SAXS: q , s , or ... h ??



Can be viewed as light S_0 reflecting off a fictitious **mirror plane**. Normal vector to plane, \vec{S}_n , is the momentum transferred.

$$\|\vec{S}\|^2 = (\vec{s} - \vec{s}_0) \cdot (\vec{s} - \vec{s}_0) = 2 - 2 \cos(2\theta) = (2 \sin(\theta))^2^*$$

$$\frac{2\pi \|\vec{S}_n\|}{\lambda} = \frac{4\pi \sin(\theta)}{\lambda} = \text{Oscillations of radiation (in radians) per unit length}$$

Sometimes called **momentum transfer**. Can have units of \AA^{-1} , or sometimes nm^{-1} .

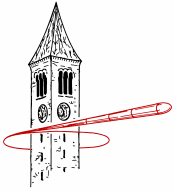
$$h = 4\pi \sin(\theta)/\lambda \quad [\text{Guinier \& Fournet (1955); Glatter \& Kratky (1982)}]$$

$$s = 4\pi \sin(\theta)/\lambda \quad [\text{Feigin \& Svergun (1987)}]$$

$$q = 4\pi \sin(\theta)/\lambda \quad [\text{Putnam, Hammel, Hura \& Tainer (2007); Jacques \& Trewhella (2010)}]$$

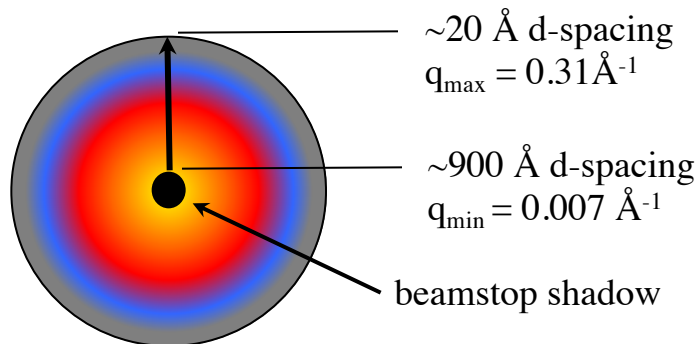
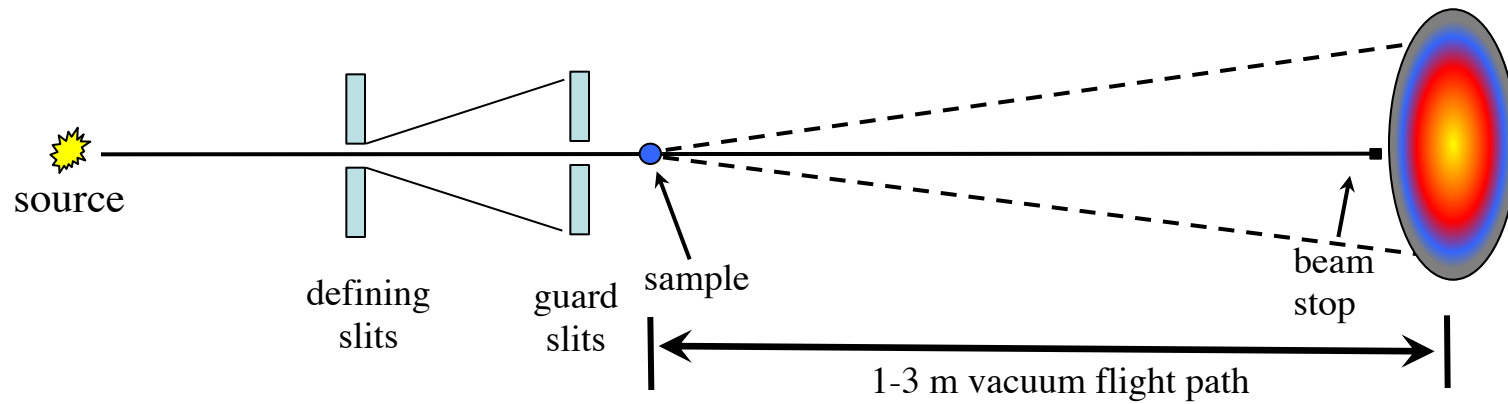
Sometimes you will see $s = 2\sin(\theta)/\lambda$ because $1/s = \text{“d-spacing”}$ (resolution in crystallography).

* $\|S\| = \|S_0\| = 1 \quad \vec{S} \cdot \vec{S}_0 = \cos(2\theta) \quad 1 - \cos(2\theta) = 2 \sin^2(\theta) \quad (\text{double-angle formula})$



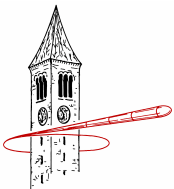
Simplified diagram of SAXS setup

typically 7-12 keV (1.7 Å - 1.0 Å). - practical high-energy limit ~20 keV



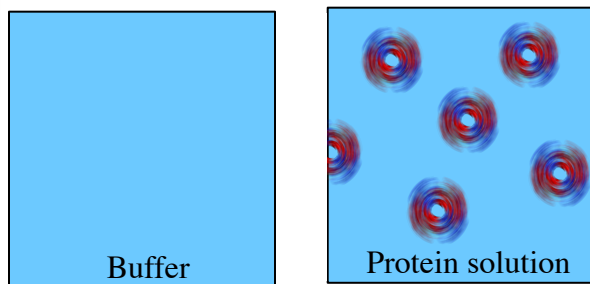
$$q = 4\pi \sin(\theta)/\lambda$$

As you get lower in scattering angle (smaller q), the background scatter gets VERY high – this ultimately limits how low you can go and how large of molecules you can study.



Real protein signal is obtained by buffer subtraction

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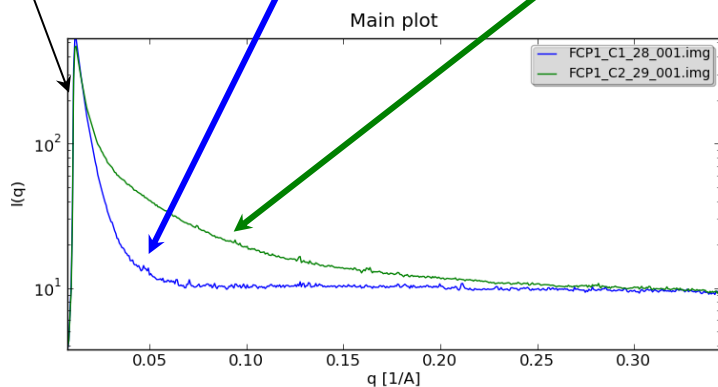


$$I_{protein} = I_{solution} - \alpha I_{buffer}$$

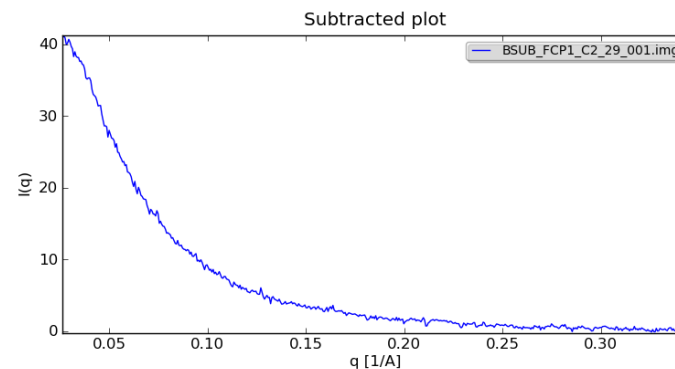
Scattering pattern for protein in vacuum is obtained by subtracting separate images normalized to the same exposure. The normalization constant α can be obtained in several ways:

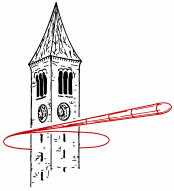
1. Assume no beam decay: $\alpha = 1$
2. Average before and after buffers
3. Scale so that tails of protein and buffer meet
4. Use transparent beamstop to integrate direct beam
- 5. Integrate beamstop diode readings**

beamstop shadow

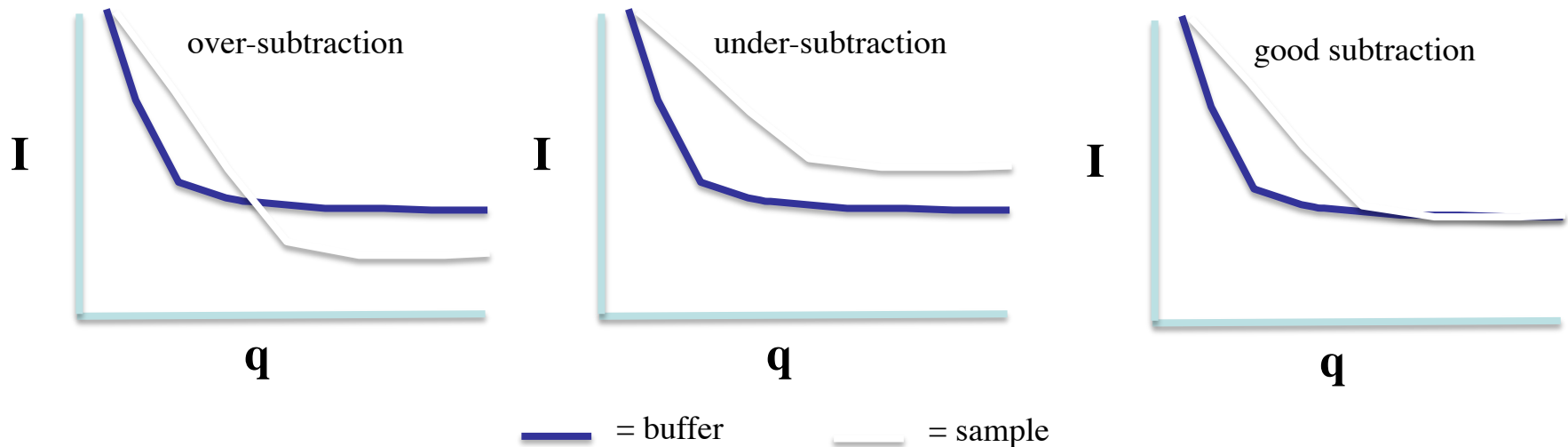


difference





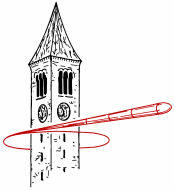
Perfect “buffer match” is everything in BioSAXS



Small changes in concentration of salts and additives can result in change of baseline scattering level

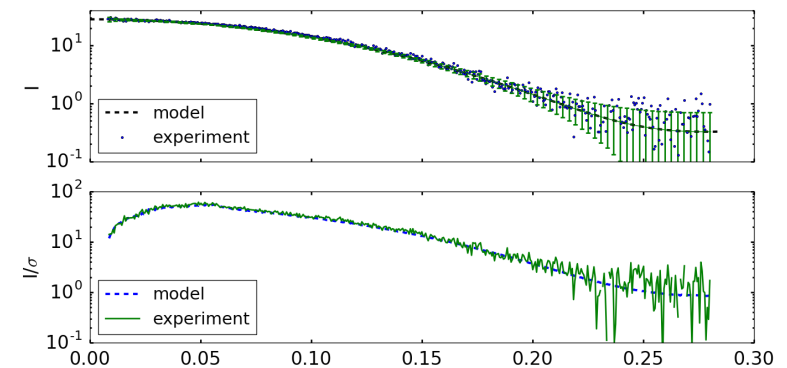
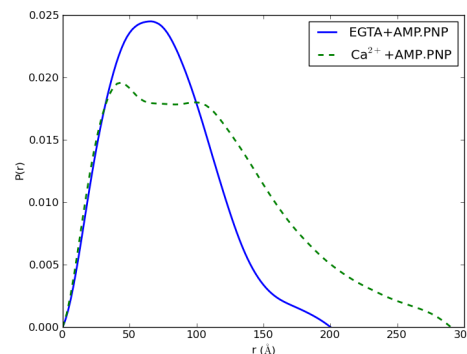
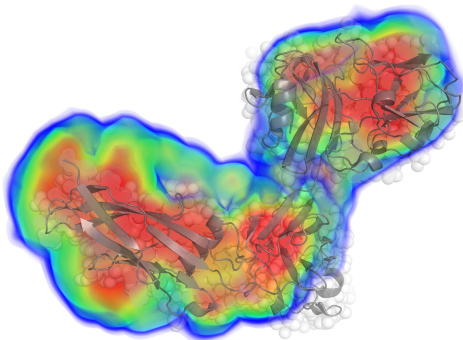
How to get matching buffer:

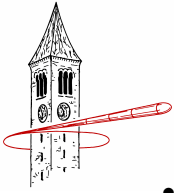
1. Use buffer from a size-exclusion chromatography run
2. Change to known buffer using centrifugal concentrator
3. Change buffer using dialysis
4. Use a “desalting” spin column



BioSAS tells you about how biomolecules behave in solution!

- quantifying **flexibility**, **disorder**, and **unfolding** in biomolecules.
- tracking of **time-resolved** structural changes (sub-milliseconds and longer)
- study of molecular crowding and **high-concentration** samples
- determination of **conformational changes** induced by binding ligands etc.
- characterizing the **ensembles** of conformations **in solution**.
- measurement of molecular weight, radius of gyration, and maximum length
- identification of physiological **oligomeric states**
- determination of structural **stability limits**
- **verification** of proposed molecular **models**
- **assembly of complexes** from known domain structures (pseudoatomic)
- calculation of true low-resolution **electron density** *in solution*.

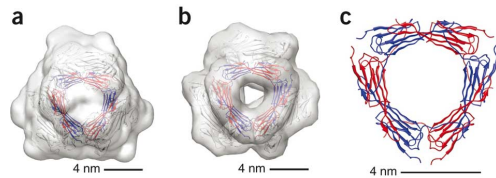




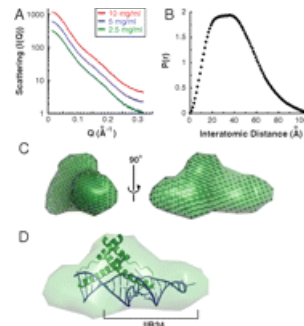
Specific Applications of BioSAXS

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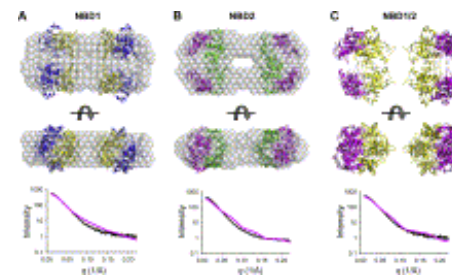
- combining NMR with SAXS to build oligomers from monomers
- **are some parts of the protein extended or disordered in solution?**
- comparing Lit vs. dark states of photoactive proteins
- comparing ligand-induced conformational changes
- adding and refining loops to homology models
- determining spatial distributions of domains connected by flexible linkers
- modeling changes in protein interaction with salt concentration and cation type
- determine fractions of monomer and dimer with change in ionic strength/additives
- categorizing discrete folded and unfolded states
- monitoring changes in protein stability with additives (stabilization due to binding)
- combining computational docking with SAXS data to improve hit rate
- building pseudoatomic models from known fragments and homology models



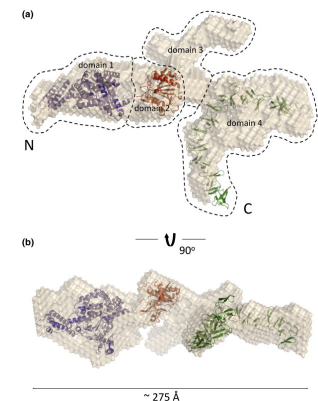
Jehle S, et al. Nat Struct Mol Biol. 2010 Sep;17(9):1037-42.



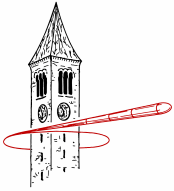
Daugherty MD, et al. Proc Natl Acad Sci U S A. 2010 Jul 13;107(28):12481-6



Park S, et al. J Struct Biol 2010 Feb; 169(2):243-51



Albesa-Jove D, et al. J Mol Biol. 2010 Mar 12;396(5):1260-70.



Sample characteristic

Purity
(monodispersity)

Oligomeric State

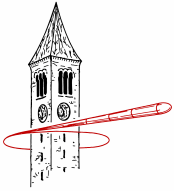
Shape/anisometry

Flexibility
Folded/Non-folded

Interparticle
Interactions

Conformation

Based on H.D.T. Mertens, D.I. Svergun / Journal of Structural Biology 172 (2010) 128–141



Sample characteristic

Basic parameter/data

Purity
(monodispersity)

Guinier plot

Oligomeric State

Particle volume,
Molecular Mass

Shape/anisometry

Envelope, R_g ,
 $P(r)$ function

Flexibility
Folded/Non-folded

Porod exponent,
Kratky plot

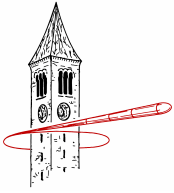
Interparticle
Interactions

Concentration
Series

Conformation

$I(q)$

Based on H.D.T. Mertens, D.I. Svergun / Journal of Structural Biology 172 (2010) 128–141



Sample characteristic

Basic parameter/data

Program/method

Purity
(monodispersity)

Guinier plot

Mixture analysis
OLIGOMER, SVD,
EFA

Oligomeric State

Particle volume,
Molecular Mass

Docking: CORAL,
FoXSDock

Shape/anisometry

Envelope, R_g,
P(r) function

Ab initio modelling
DAMMIF, DENSS

Flexibility
Folded/Non-folded

Porod exponent,
Kratky plot

Mult. conformations
SCATTER, EOM

Interparticle
Interactions

Concentration
Series

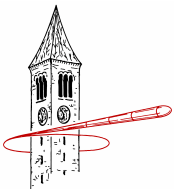
Interaction
potentials

Conformation

I(q)

Compare to model
Crysol, FoxS

Based on H.D.T. Mertens, D.I. Svergun / Journal of Structural Biology 172 (2010) 128–141



Example of SAXS titration and model validation

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Thomas, W.C., Brooks, F.P., Burnim, A.A. *et al.* Convergent allostery in ribonucleotide reductase. *Nat Commun* **10**, 2653 (2019).
<https://doi.org/10.1038/s41467-019-10568-4>

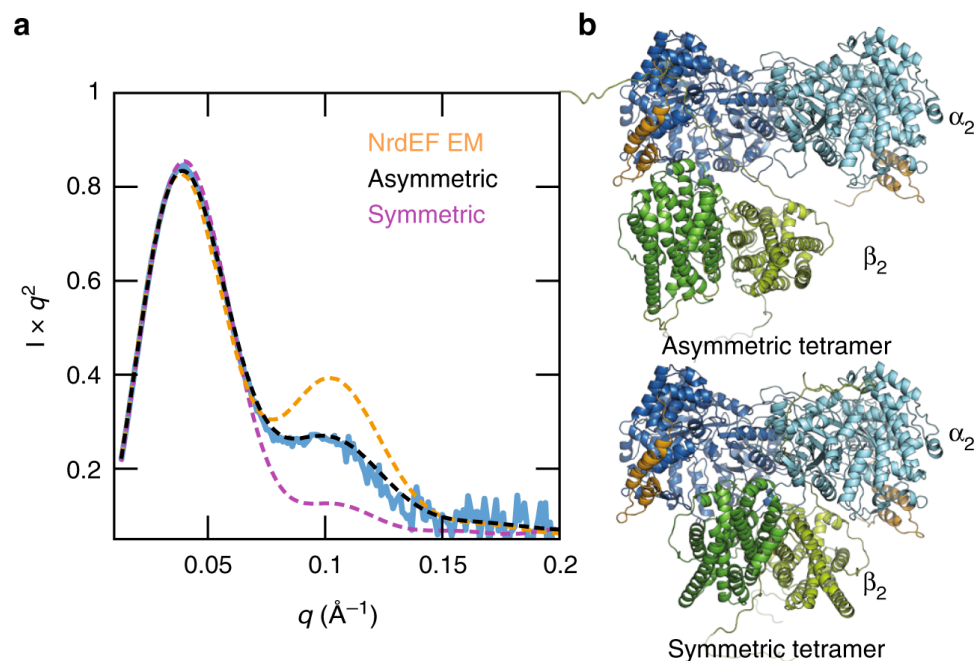
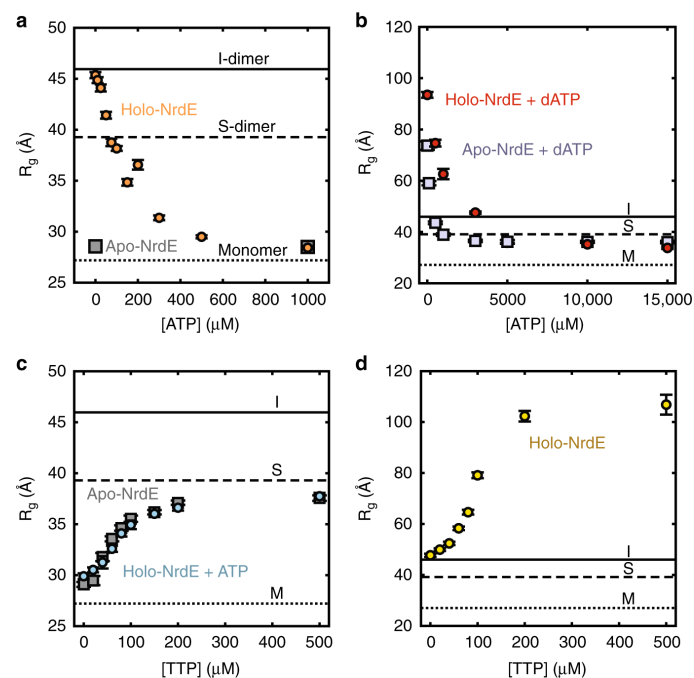
Study combines:

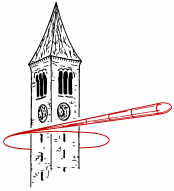
- SAXS
- cryoEM
- crystallography

“Reversible interconversion of six unique structures ... conformational gymnastics necessary for RNR activity”

Watching R_g of a complex change while titrating in ATP:

Comparing models to data:





Example of how basic SAXS data complement a larger study

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[BMC Biol.](#) 2018 Jul 11;16(1):76.

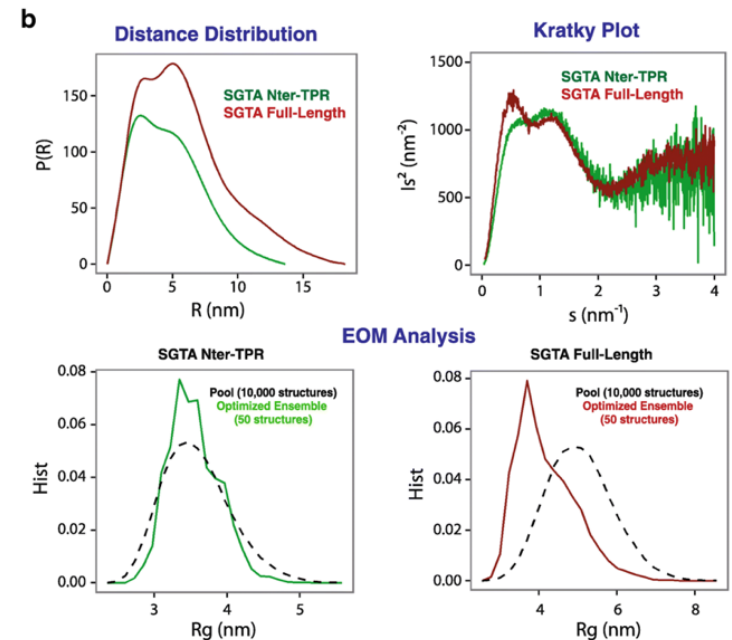
Structural complexity of the co-chaperone SGTA: a conserved C-terminal region is implicated in dimerization and substrate quality control.

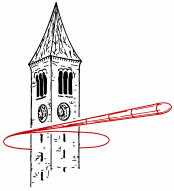
[Martínez-Lumbreras S](#)¹, [Kryzstofinska EM](#)¹, [Thapaliya A](#)¹, [Spilotros A](#)², [Matak-Vinkovic D](#)³, [Salvadori E](#)^{4,5}, [Roboti P](#)⁶, [Nyathi Y](#)^{6,7}, [Muench JH](#)¹, [Roessler MM](#)⁴, [Svergun DI](#)², [High S](#)⁶, [Isaacson RL](#)⁸.

- Confirmed dimeric state
- $P(r)$ function confirms domains with 5 nm separation
- $P(r)$ also confirms full-length protein is more compact than truncated
- Kratky indicates moderate flexibility
- EOM also shows how full-length construct is more compact

SAXS combined with

- Native mass spectrometry (shows dimer in solution)
- NMR
- EPR spectroscopy (DEER)
- DLS
- CD





Example of sophisticated pseudoatomic homology model building and refinement

oxygen-sensing FixL-FixJ

(Wright *et al. Sci. Signal.* 11 10 April 2018)

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Data from:

- crystallography
- SEC-SAXS
- Existing fragments from PDB
- homology modeling
- Validation of part of model via SAXS on truncated protein

Software:

- JPred, Coils (which parts are helices vs coils)
- PEP-FOLD generate models of linkers
- Torsion angle MD in CNS to refine positions of domains and loops
- SWISS-MODEL to generate homology model
- HADDOCK to refine and dock domains
- pyDockSAXS and FoXS-Dock for placement of domains
- FTDock/Crysol and PatchDock/FoXS

